

# Key!

## One to One Functions and Graphs of Inverses Practice

$$x = 3y - 2$$

Graph the following Functions AND their inverses. Are the original functions one to one??

1)  $f(x) = 3x - 2$

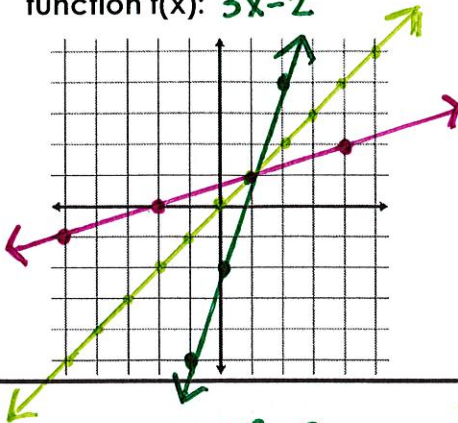
function  $f(x): 3x - 2$

inverse  $f^{-1}(x): \frac{x+2}{3}$

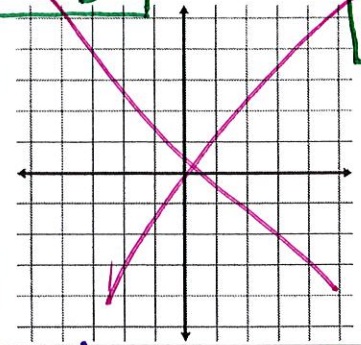
$$\frac{3y}{3} = \frac{x+2}{3}$$

$$y = \frac{x+2}{3}$$

| x  | y  |
|----|----|
| -1 | -5 |
| 0  | -2 |
| 1  | 1  |
| 2  | 4  |



| x  | y  |
|----|----|
| -5 | -1 |
| -2 | 0  |
| 1  | 1  |
| 4  | 2  |



one to one?  
Yes!

2)  $f(x) = x^2 - 2$

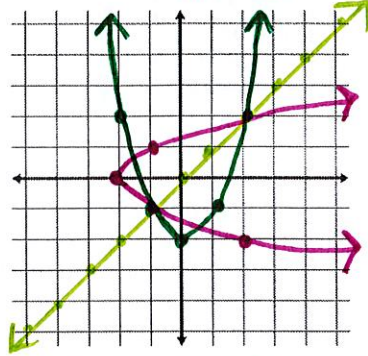
function  $f(x): x^2 - 2$

\* not a function!  
inverse  $f^{-1}(x): \pm\sqrt{x+2}$

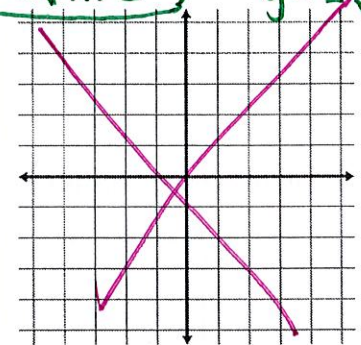
$$\sqrt{x+2} = y^2$$

$$y = \pm\sqrt{x+2}$$

| x  | y  |
|----|----|
| -2 | 2  |
| -1 | -1 |
| 0  | -2 |
| 1  | -1 |
| 2  | 2  |



| x  | y  |
|----|----|
| 2  | -2 |
| -1 | -1 |
| -2 | 0  |
| -1 | 1  |
| 2  | 2  |



one to one?  
No!

3)  $f(x) = x^3 + 2$

function  $f(x): x^3 + 2$

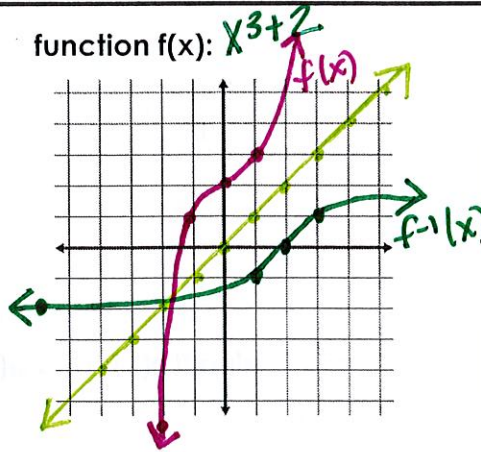
inverse  $f^{-1}(x): \sqrt[3]{x-2}$

$$x = y^3 + 2$$

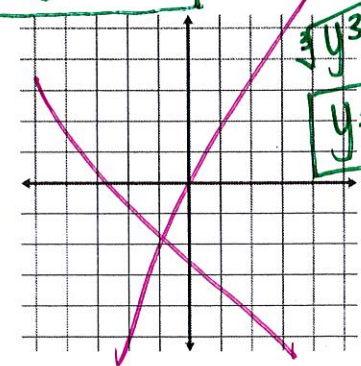
$$\sqrt[3]{y^3} = \sqrt[3]{x-2}$$

$$y = \sqrt[3]{x-2}$$

| x  | y  |
|----|----|
| -2 | -6 |
| -1 | 1  |
| 0  | 2  |
| 1  | 3  |
| 2  | 10 |



| x  | y  |
|----|----|
| -6 | -2 |
| 1  | -1 |
| 2  | 0  |
| 3  | 1  |
| 10 | 2  |



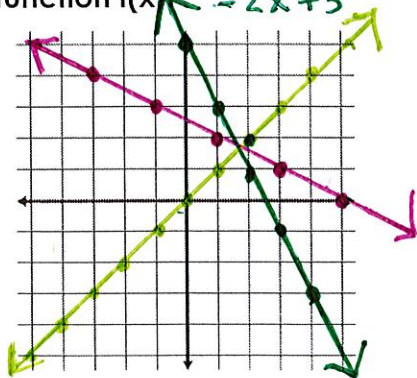
one to one?  
Yes!

4)  $f(x) = -2x + 5$

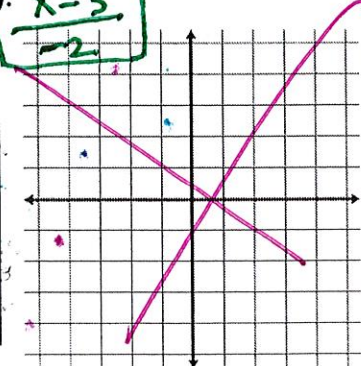
function  $f(x): -2x + 5$

inverse  $f^{-1}(x): \frac{x-5}{-2}$

| x | y  |
|---|----|
| 4 |    |
| 3 |    |
| 2 |    |
| 1 |    |
| 0 | 5  |
| 1 | 3  |
| 2 | 1  |
| 3 | -1 |
| 4 | -3 |
| 5 | -5 |



| x  | y |
|----|---|
| 5  | 0 |
| 3  | 1 |
| 1  | 2 |
| -1 | 3 |
| -3 | 4 |
| -5 | 5 |



one to one?  
Yes!

$$x = -2y + 5$$

$$\frac{-2}{-2}y = \frac{x-5}{-2}$$